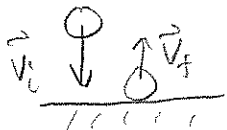


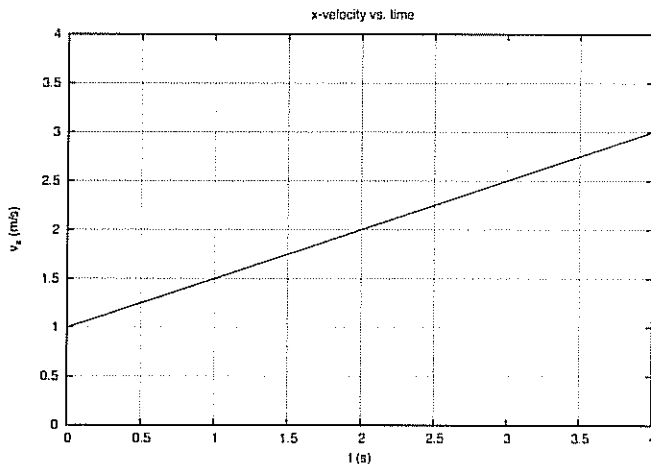
You must include units with all quantities (that have units). You must explain reasoning or show work for all questions.

1. [5] A golf ball is dropped vertically onto a table top and bounces. Just before it hits the table, its velocity is  $(0, -4, 0)$  m/s. After hitting the table, its velocity is  $(0, 3, 0)$  m/s. What is the coefficient of restitution of the golf ball?



$$C_R = \left| \frac{v_{f\perp}}{v_{i\perp}} \right| = \frac{3}{4} = 0.75$$

2. You analyze a video of a fancart on a track, and the x-velocity of the fancart as a function of time looks like the graph below.



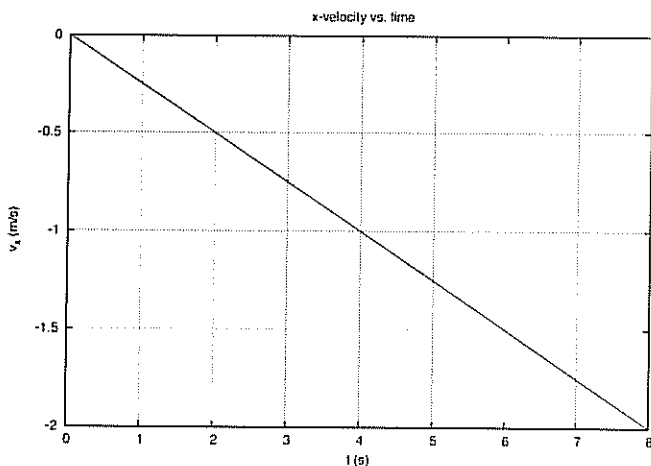
- [5](a) What is the x-acceleration of the fancart? Be sure to show your calculation or explain how you determined your answer.

$$a_x = \text{slope} = \frac{3 - 1 \frac{\text{m}}{\text{s}}}{4 - 0 \text{ s}} = \frac{2}{4} \frac{\text{m}}{\text{s}^2} = 0.5 \frac{\text{m}}{\text{s}^2}$$

- [5](b) Is the cart speeding up or slowing down? Explain your reasoning.

$v_x$  is + and  $a_x$  is +, so the cart is speeding up.

3. You analyze a video of a fancart on a track, and the x-velocity of the fancart as a function of time looks like the graph below.



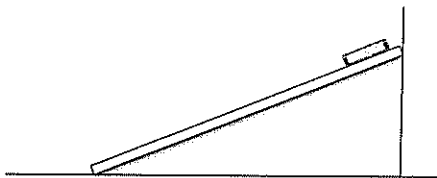
- [5](a) What is the x-acceleration of the fancart? Be sure to show your calculation or explain how you determined your answer.

$$a_x = \text{slope} = \frac{(-2 - 0 \frac{m}{s})}{8 - 0 s} = -\frac{1}{4} \frac{m}{s^2} = -0.25 \frac{m}{s^2}$$

- [5](b) Is the cart speeding up or slowing down? Explain your reasoning.

$v_x$  is - and  $a_x$  is -, so the cart is speeding up.

4. Suppose that you set up an inclined track and a cart as shown below. (This is exactly like the apparatus for the Newton's Second Law experiment that you did in class.)



- [5](a) If you add metal bars to the car and double the mass, what must you do in order to keep the net force on the cart the same?

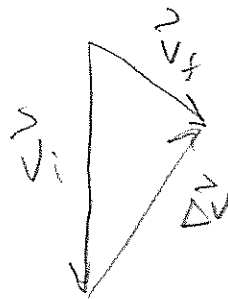
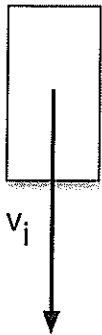
- (a) increase the angle of inclination
- (b) decrease the angle of inclination
- (c) nothing; adding mass will not change the net force on the cart

- [5](b) Explain your reasoning to the question above.

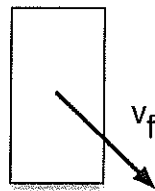
$\vec{F}_{\text{net}} = m\vec{a}$  if  $\vec{F}_{\text{net}}$  stays then doubling mass requires decreasing  $\vec{a}$  by  $\frac{1}{2}$ . Thus, decrease the angle of the ramp.

5. In a Lunar Lander game, at some instant of time, the lunar module <sup>has</sup> a velocity  $\vec{v}_i$  shown below. At a later time, the module has the velocity  $\vec{v}_f$ .

[5](a) What is the direction of the net force on the lunar module? (Your answer should be an arrow that represents the net force vector. You must sketch a picture that correctly illustrates how to determine the direction of the net force?)



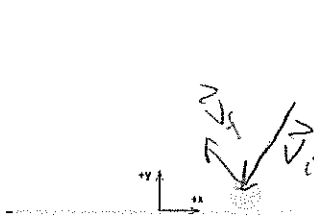
$\vec{a}$  and  $\vec{F}_{net}$  are in same dir as  $\Delta \vec{v}$ , up and to the right.



[5](b) Did the lunar module speed up or slow down during this time interval? Explain your reasoning.

It slowed down because  $|\vec{v}_f| < |\vec{v}_i|$  as indicated by the length of the arrows.

6. (BONUS) A basketball bounces on the floor. Just before hitting the floor, its velocity is  $(-2, -3, 0)$  m/s. Just after hitting the floor, its velocity is  $(-1.5, 1.5, 0)$  m/s.



$$\vec{v}_i = (-2, -3, 0) \frac{m}{s}$$

$$\vec{v}_f = (-1.5, 1.5, 0) \frac{m}{s}$$

[5](a) What is the coefficient of restitution of the basketball?

$$C_R = \left| \frac{v_{f \perp}}{v_{i \perp}} \right| = \left| \frac{1.5}{3} \right| = 0.5$$

[5](b) In what direction is the frictional force on the basketball? (to the right or to the left) You must explain your reasoning.

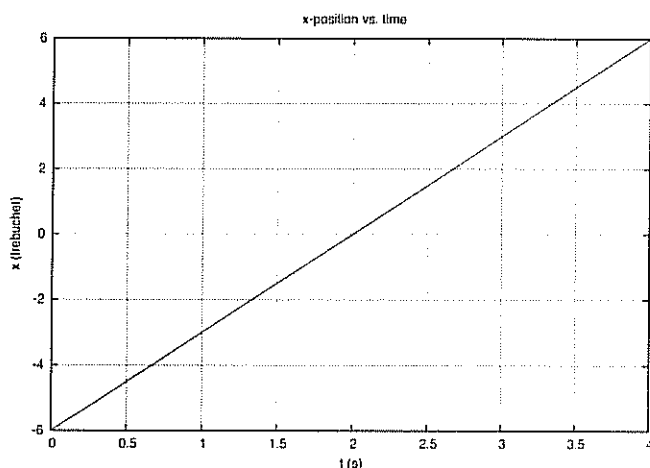
friction causes  $v_{\parallel}$  to change. In this case,  $v_{\parallel} \approx v_x$  and  $v_x$  decreases from  $-\frac{2}{3} \frac{m}{s}$  to  $-\frac{1.5}{3} \frac{m}{s}$ . Thus friction acts to the right, causing  $v_x$  to slow down.

7. Suppose that there is a new game that is like angry birds except that you use a trebuchet to shoot angry water buffaloes. You capture a video of the motion of the water buffalo, and you use the the *trebuchet* as the standard unit of length. You find that the free-fall y-acceleration in the world of the game is  $-4 \text{ trebuchets/s}^2$ .

[5](a) Using  $\vec{g} \approx (0, -10, 0) \text{ m/s}^2$  for Earth, how many meters long is 1 trebuchet if we assume that the game's world is Earth?

$$\frac{-10 \text{ m/s}^2}{-4 \text{ treb/s}^2} = 2.5 \frac{\text{m}}{\text{treb}} \quad \text{so } 1 \text{ treb. is } 2.5 \text{ m long. } \checkmark$$

[5](b) You use video analysis to determine the  $x(t)$  graph for a water buffalo and obtain the graph below. Note that the unit for position is *trebuchet*.



What is the x-velocity of the water buffalo in *trebuchet/s*?

$$v_x = \text{slope} = \frac{6 - (-6) \text{ treb}}{4 - 0 \text{ s}} = \frac{12 \text{ treb}}{4 \text{ s}} = 3 \frac{\text{treb}}{\text{s}}$$

[5](c) Use your scaling factor from part (a) to determine the x-velocity in m/s.

$$v_x = \left( 3 \frac{\text{treb}}{\text{s}} \right) \left( \frac{2.5 \text{ m}}{1 \text{ treb}} \right) = 7.5 \frac{\text{m}}{\text{s}}$$

Section 2. Iterative Method of Applying Newton's Second Law

8. [20] A 0.045-kg golf ball is at the position  $(-15, 0, 0)$  m on a level green when it is putted. Its velocity immediately after leaving the putter is  $(8, 0, 0)$  m/s. There is a constant frictional force by the grass on the ball as it rolls that is  $(-0.09, 0, 0)$  N. Use the iterative method to find the velocity and position of the golf ball at the following times:  $t = 0.25$  s,  $t = 0.5$  s,  $t = 0.75$  s,  $t = 1.0$  s. Show your work and neatly record your answer in a data table with three columns for  $t$ , *velocity*, and *position*. Write the positions and velocities as vectors.

$$\vec{r}_i = (-15, 0, 0) \text{ m} \quad \Delta t = 0.25 \text{ s}$$

$$\vec{v}_i = (8, 0, 0) \frac{\text{m}}{\text{s}}$$

$$\vec{F}_{\text{net}} = (-0.09, 0, 0) \text{ N}$$

$$m = 0.045 \text{ kg}$$

$$t = 0.25 \text{ s} : \quad \vec{v} = (8, 0, 0) + \left( \frac{(-0.09, 0, 0) \text{ N}}{0.045 \text{ kg}} \right) (0.25 \text{ s}) = (7.5, 0, 0) \frac{\text{m}}{\text{s}}$$

$$\vec{r} = (-15, 0, 0) + (7.5, 0, 0)(0.25 \text{ s}) = (-13.125, 0, 0) \text{ m}$$

$t$	$\vec{r}$ (m)	$\vec{v}$ ( $\frac{\text{m}}{\text{s}}$ )
0	$(-15, 0, 0)$	$(8, 0, 0)$
0.25	$(-13.125, 0, 0)$	$(7.5, 0, 0)$
0.5	$(-11.375, 0, 0)$	$(7, 0, 0)$
0.75	$(-9.75, 0, 0)$	$(6.5, 0, 0)$
1.0	$(-8.25, 0, 0)$	$(6, 0, 0)$

### Section 3. LAB

9. [20] Go to our course web site and download the video *toy-car.mov*. Use Tracker to analyze its motion.  
Sign: "I answered this question on my own without using any person or resource except my lab notebook and the Tracker software."

Signature: \_\_\_\_\_

- (a) When the car is speeding up and traveling to the right, what is (approximately) its acceleration? Give your answer and describe how you determined it.

$$\text{slope of } v_x \text{ vs. } t \text{ is } \approx 0.31 \frac{\text{m}}{\text{s}}$$

For part (a), what is the direction of the net force on the car during this time interval? Explain your reasoning.

$a_x$  is + so  $F_{net,x}$  is + and  $\vec{F}_{net}$  is in +x dir.  
 $\vec{F}_{net}$  is prop. to  $\vec{a}$  according to Newton's 2<sup>nd</sup> law

- (b) At what time is the car at rest? Give your answer and describe how you determined it.

at rest is  $v_x = 0$  which occurs at  $t = 2.05$  to  
 $t = 2.335$

- (c) When the car is traveling to the right and slowing down, what is (approximately) its acceleration? Give your answer and describe how you determined it.

$$a_x = \text{slope} = -0.77 \frac{\text{m}}{\text{s}^2}$$

For part (c), what is the direction of the net force on the car during this time interval? Explain your reasoning.

$\vec{F}_{net}$  is in -x dir. since  $a_x$  is negative.